Eighth Problem of the Week, due Thursday 04/11 11:59pm

On a 10×10 board, a positive integer is written in each square so that the difference between the numbers placed in adjacent squares is always less than or equal to 1. (Two squares are adjacent if they have a common side).

Find a board that has as many different numbers as possible.