

Sixth Problem of the Week, due Thursday 10/19

Let $f(x)$ be a polynomial of degree n with n distinct real roots. Prove that the polynomial

$$f(x)f''(x) - (f'(x))^2$$

has no real roots.

Hint: Consider the derivative of a certain function.