Eighth Problem of the Week, due Thursday 11/02

Let x, y, z be positive real numbers such that $x^2 + y^2 + z^2 = 1$. Show that

$$x^2yz + xy^2z + xyz^2 \le \frac{1}{3}$$

Hint: The inequality of arithmetic and geometric means, AM-GM Inequality, might be helpful.